# Package 'nett'

November 9, 2022

**Title** Network Analysis and Community Detection

**Version** 1.0.0

**Description** Features tools for the network data analysis and community detection.
Provides multiple methods for fitting, model selection and goodness-of-fit testing in degree-corrected stochastic blocks models.
Most of the computations are fast and scalable for sparse networks, esp. for Poisson versions of the models.
Implements the following:
Amini, Chen, Bickel and Levina (2013) <doi:10.1214/13-AOS1138>
Bickel and Sarkar (2015) <doi:10.1111/rssb.12117>
Lei (2016) <doi:10.1214/15-AOS1370>
Wang and Bickel (2017) <doi:10.1214/16-AOS1457>
Zhang and Amini (2020) <arXiv:2012.15047>
Le and Levina (2022) <doi:10.1214/21-EJS1971>.

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**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 7.2.1

**Suggests** testthat, knitr, rmarkdown, igraph, ggplot2, dplyr, tidyr, tibble, mixtools, EnvStats, purrr, RSpectra

**Depends** R (>= 2.10)

**Imports** magrittr, Rcpp, Matrix, foreach, methods, stats, grDevices, graphics

**LinkingTo** Rcpp, RcppArmadillo

**VignetteBuilder** knitr

**URL** https://github.com/aaamini/nett

**BugReports** https://github.com/aaamini/nett/issues

**NeedsCompilation** yes

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`adj_spec_test` *Adjusted spectral test*

## Description

The adjusted spectral goodness-of-fit test based on Poisson DCSBM.

The test is a natural extension on Lei's work of testing goodness-of-fit for SBM. The residual matrix $\tilde{A}$ is computed from the DCSBM estimation expectation of `A`. To speed up computation, the residual matrix uses Poisson variance instead. Specifically,

$$\tilde{A}_{ij} = (A_{ij} - \hat{P}_{ij})/(n\hat{P}_{ij})^{1/2}, \quad \hat{P}_{ij} = \hat{\theta}_i\hat{\theta}_j\hat{B}_{\hat{z}_i,\hat{z}_j} \cdot 1\{i \neq j\}$$

where $\hat{\theta}$ and $\hat{B}$ are computed using estim_dcsbm if not provided.

Adjusted spectral test

## Usage

```
adj_spec_test(
  A,
  K,
  z = NULL,
  DC = TRUE,
  theta = NULL,
  B = NULL,
  cluster_fct = spec_clust,
  ...
)
```

## Arguments

| | |
|---|---|
| `A` | adjacency matrix. |
| `K` | number of communities. |
| `z` | label vector for rows of adjacency matrix. If not given, will be calculated by the spectral clustering. |
| `DC` | whether or not include degree correction in the parameter estimation. |
| `theta` | give the propensity parameter directly. |
| `B` | give the connectivity matrix directly. |
| `cluster_fct` | community detection function to get `z` , by default using spec_clust. |
| `...` | additional arguments for `cluster_fct`. |

## Value

Adjusted spectral test statistics.

## References

Details of modification can be seen at Adjusted chi-square test for degree-corrected block models, Linfan Zhang, Arash A. Amini, arXiv preprint arXiv:2012.15047, 2020.

The original spectral test is from A goodness-of-fit test for stochastic block models Lei, Jing, Ann. Statist. 44 (2016), no. 1, 401–424. doi:10.1214/15-AOS1370.

---

`bethe_hessian_select` *Beth-Hessian model selection*

---

## Description

Estimate the number of communities under block models by using the spectral properties of network Beth-Hessian matrix with moment correction.

## Usage

```
bethe_hessian_select(A, Kmax)
```

## Arguments

| | |
|---|---|
| `A` | adjacency matrix. |
| `Kmax` | the maximum number of communities to check. |

## Value

A list of result

| | |
|---|---|
| `K` | estimated the number of communities |
| `rho` | eigenvalues of the Beth-Hessian matrix |

## References

Estimating the number of communities in networks by spectral methods, Can M. Le, Elizaveta Levina, arXiv preprint arXiv:1507.00827, 2015

## compute_block_sums *Block sum of an adjacency matrix*

### Description

Compute the block sum of an adjacency matrix given a label vector.

### Usage

```
compute_block_sums(A, z)
```

### Arguments

| | |
|---|---|
| A | adjacency matrix. |
| z | label vector. |

### Value

A K x L matrix with (k,l)-th element as $sum_{i,j} A_{i,j} 1 z_i = k, z_j = l$

## compute_confusion_matrix *Compute confusion matrix*

### Description

Compute confusion matrix

### Usage

```
compute_confusion_matrix(z, y, K = NULL)
```

### Arguments

| | |
|---|---|
| z | a label vector |
| y | a label vector |
| K | number of labels in both z and y |

### Value

A KxK confusion matrix between z and y

## compute_mutual_info *Compute normalized mutual information (NMI)*

### Description

Compute the NMI between two label vectors with the same cluster number

### Usage

```
compute_mutual_info(z, y)
```

### Arguments

| | |
|---|---|
| z | a label vector |
| y | a label vector |

### Value

NMI between z and y

## estim_dcsbm *Estimate model parameters of a DCSBM*

### Description

Compute the block sum of an adjacency matrix given a label vector.

### Usage

```
estim_dcsbm(A, z)
```

### Arguments

| | |
|---|---|
| A | adjacency matrix. |
| z | label vector. |

### Details

$$\hat{B}_{k\ell} = \frac{N_{k\ell}(\hat{z})}{m_{k\ell}(\hat{z})}, \quad \hat{\theta}_i = \frac{n_{\hat{z}_i}(\hat{z}) d_i}{\sum_{j:\hat{z}_j=\hat{z}_i} d_i}$$

where $N_{k\ell}(\hat{z})$ is the sum of the elements of A in block $(k, \ell)$ specified by labels $\hat{z}$, $n_k(\hat{z})$ is the number of nodes in community $k$ according to $\hat{z}$ and $m_{k\ell}(\hat{z}) = n_k(\hat{z})(n_\ell(\hat{z}) - 1\{k = \ell\})$

### Value

A list of result

| | |
|---|---|
| B | estimated connectivity matrix. |
| theta | estimated node propensity parameter. |

---

`eval_dcsbm_bic` *Compute BIC score*

---

### Description

compute BIC score when fitting a DCSBM to network data

### Usage

```
eval_dcsbm_bic(A, z, K, poi)
```

### Arguments

| | |
|---|---|
| A | adjacency matrix |
| z | label vector |
| K | number of community in z |
| poi | whether to use Poisson version of likelihood |

### Details

the BIC score is calculated by -2*log likelihood minus $K \times (K+1) \times log(n)$

### Value

BIC score

### References

BIC score is originally proposed in Likelihood-based model selection for stochastic block models Wang, YX Rachel, Peter J. Bickel, The Annals of Statistics 45, no. 2 (2017): 500-528.

The details of modified implementation can be found in Adjusted chi-square test for degree-corrected block models, Linfan Zhang, Arash A. Amini, arXiv preprint arXiv:2012.15047, 2020.

### See Also

eval_dcsbm_like, eval_dcsbm_loglr

`eval_dcsbm_like` *Log likelihood of a DCSBM (fast with poi = TRUE)*

## Description

Compute the log likelihood of a DCSBM, using estimated parameters B, theta based on the given label vector

## Usage

```
eval_dcsbm_like(A, z, poi = TRUE, eps = 1e-06)
```

## Arguments

| | |
|---|---|
| `A` | adjacency matrix |
| `z` | label vector |
| `poi` | whether to use Poisson version of likelihood |
| `eps` | truncation threshold for the Bernoulli likelihood, used when parameter phat is close to 1 or 0. |

## Details

The log likelihood is calculated by

$$\ell(\hat{B}, \hat{\theta}, \hat{\pi}, \hat{z} \mid A) = \sum_i \log \hat{\pi}_{z_i} + \sum_{i<j} \phi(A_{ij}; \hat{\theta}_i \hat{\theta}_j \hat{B}_{\hat{z}_i \hat{z}_j})$$

where $\hat{B}$, $\hat{\theta}$ is calculated by estim_dcsbm, $\hat{\pi}_k$ is the proportion of nodes in community k.

## Value

log likelihood of a DCSBM

## See Also

eval_dcsbm_loglr, eval_dcsbm_bic

`eval_dcsbm_loglr` *Log-likelihood ratio of two DCSBMs (fast with poi = TRUE)*

## Description

Computes the log-likelihood ratio of one DCSBM relative to another, using estimated parameters `B` and `theta` based on the given label vectors.

## Usage

```
eval_dcsbm_loglr(A, labels, poi = TRUE, eps = 1e-06)
```

## Arguments

| | |
|---|---|
| `A` | adjacency matrix |
| `labels` | a matrix with two columns representing two different label vectors |
| `poi` | whether to use Poisson version of likelihood (instead of Bernoulli) |
| `eps` | truncation threshold for the Bernoulli likelihood, used when parameter phat is close to 1 or 0. |

## Details

The log-likehood ratio is computed between two DCSBMs specified by the columns of `labels`. The function computes the log-likelihood ratio of the model with `labels[ , 2]` w.r.t. the model with `labels[ , 1]`. This is often used with two label vectors fitted using different number of communities (say `K` and `K+1`).

When `poi` is set to `TRUE`, the function uses fast sparse matrix computations and is scalable to large sparse networks.

## Value

log-likelihood ratio

## See Also

eval_dcsbm_like, eval_dcsbm_bic

## extract_largest_cc *Extract largest component*

### Description

Extract the largest connected component of a network

### Usage

```
extract_largest_cc(gr, mode = "weak")
```

### Arguments

| | |
|---|---|
| gr | The network as an igraph object |
| mode | Type of connected component ("weak"\|"strong") |

### Value

An igraph object

## extract_low_deg_comp *Extract low-degree component*

### Description

Extract a low-degree connected component of a network

### Usage

```
extract_low_deg_comp(g, deg_prec = 0.75, verb = FALSE)
```

### Arguments

| | |
|---|---|
| g | The network as an igraph object |
| deg_prec | The cut-off degree percentile |
| verb | Whether to be verbose (TRUE\|FALSE) |

### Value

An igraph object

`fast_cpl` *CPL algorithm for community detection (fast)*

## Description

The Conditional Pseudo-Likelihood (CPL) algorithm for fitting degree-corrected block models

## Usage

```
fast_cpl(Amat, K, ilabels = NULL, niter = 10)
```

## Arguments

| | |
|---|---|
| `Amat` | adjacency matrix of the network |
| `K` | desired number of communities |
| `ilabels` | initial label vector (if not provided, initial labels are estimated using spec_clust) |
| `niter` | number of iterations |

## Details

The function implements the CPL algorithm as described in the paper below. It relies on the `mixtools` package for fitting a mixture of multinomials to a block compression of the adjacency matrix based on the estimated labels and then reiterates.

Technically, `fast_cpl` fits a stochastic block model (SBM) conditional on the observed node degrees,to account for the degree heterogeneity within communities that is not modeled well in SBM. CPL can also be used to effectively estimate the parameters of the degree-corrected block model (DCSBM).

The code is an adaptation of the original R code by Aiyou Chen with slight simplifications.

## Value

Estimated community label vector.

## References

For more details, see Pseudo-likelihood methods for community detection in large sparse networks, A. A. Amini, A. Chen, P. J. Bickel, E. Levina, Annals of Statistics 2013, Vol. 41 (4), 2097—2122.

## Examples

```
head(fast_cpl(igraph::as_adj(polblogs), 2), 50)
```

## fast_sbm *Sample from a SBM (fast)*

### Description

Samples an adjacency matrix from a stochastic block model (SBM)

### Usage

```
fast_sbm(z, B)
```

### Arguments

| | |
|---|---|
| z | Node labels ($n * 1$) |
| B | Connectivity matrix ($K * K$) |

### Details

The function implements a fast algorithm for sampling sparse SBMs, by only sampling the necessary nonzero entries. This function is adapted almost verbatim from the original code by Aiyou Chen.

### Value

An adjacency matrix following SBM

### Examples

```
B = pp_conn(n = 10^4, oir = 0.1, lambda = 7, pri = rep(1,3))$B
head(fast_sbm(sample(1:3, 10^4, replace = TRUE), B))
```

## gen_rand_conn *Generate randomly permuted connectivity matrix*

### Description

Creates a randomly permuted DCPP connectivity matrix with a given average expected degree

### Usage

```
gen_rand_conn(n, K, lambda, gamma = 0.3, pri = rep(1, K)/K, theta = rep(1, n))
```

### Arguments

| | |
|---|---|
| n | number of nodes |
| K | number of communities |
| lambda | expected average degree |
| gamma | a measure of out-in-ratio (convex combination parameter) |
| pri | the prior on community labels |
| theta | node connection propensity parameter of DCSBM, by default E(theta) = 1 |

### Details

The connectivity matrix is a convex combination of a random symmetric permutation matrix and the matrix of all ones, with weights gamm and 1-gamma.

### Value

connectivity matrix B of the desired DCSBM.

---

## get_dcsbm_exav_deg *Calculate the expected average degree of a DCSBM*

---

### Description

Calculate the expected average degree of a DCSBM

### Usage

```
get_dcsbm_exav_deg(n, pri, B, ex_theta = 1)
```

### Arguments

| | |
|---|---|
| n | number of nodes |
| pri | distribution of node labels (K x 1) |
| B | connectivity matrix (K x K) |
| ex_theta | expected value of theta |

### Value

expected average degree of a DCSBM

## label_mat2vec *Convert label matrix to vector*

### Description

Convert label matrix to vector

### Usage

```
label_mat2vec(Z)
```

### Arguments

| | |
|---|---|
| Z | a cluster assignment matrix |

### Value

A label vector that follows the assignment matrix

## label_vec2mat *Convert label vector to matrix*

### Description

Convert label vector to matrix

### Usage

```
label_vec2mat(z, K = NULL, sparse = FALSE)
```

### Arguments

| | |
|---|---|
| z | a label vector |
| K | number of labels in z |
| sparse | whether the output should be sparse matrix |

### Value

A cluster assignment matrix that follows from the label vector z

nac_test *NAC test*

## Description

The NAC test to measure the goodness-of-fit of the DCSBM to network data.

The function computes the NAC+ or NAC statistics in the paper below. Label vectors, if not provided, are estimated using spec_clust by default but one can also use any other community detection algorithms through `cluster_fct`. Note that the function has to have `A` and `K` as its first two arguments, and additional arguments could be provided through `...`.

## Usage

```
nac_test(A, K, z = NULL, y = NULL, plus = TRUE, cluster_fct = spec_clust, ...)
```

## Arguments

| | |
|---|---|
| `A` | adjacency matrix. |
| `K` | number of communities. |
| `z` | label vector for rows of `A`. If not provided, will be estimated from `cluster_fct`. |
| `y` | label vector for columns of `A`. If not provided, will be estimated from `cluster_fct`. |
| `plus` | whether or not use column label vector with (`K`+1) communities, default is TRUE. |
| `cluster_fct` | community detection function to get `z` and `y`, by default using spec_clust. The first two arguments have to be `A` and `K`. |
| `...` | additional arguments for `cluster_fct`. |

## Value

A list of result

| | |
|---|---|
| `stat` | NAC or NAC+ test statistic. |
| `z` | row label vector. |
| `y` | column label vector. |

## References

Adjusted chi-square test for degree-corrected block models, Linfan Zhang, Arash A. Amini, arXiv preprint arXiv:2012.15047, 2020.

## See Also

snac_test

## Examples

```
A <- sample_dcpp(500, 10, 4, 0.1)$adj
nac_test(A, K = 4)$stat
nac_test(A, K = 4, cluster_fct = fast_cpl)$stat
```

---

`plot_deg_dist` *Plot degree distribution*

---

## Description

Plot the degree distribution of a network on log scale

## Usage

```
plot_deg_dist(gr, logx = TRUE)
```

## Arguments

| | |
|---|---|
| `gr` | the network as an igraph object |
| `logx` | whether the degree is in log scale. |

## Value

Histogram of the degree of 'gr'.

---

`plot_net` *Plot a network*

---

## Description

Plot a network using degree-modulated node sizes, community colors and other enhancements

## Usage

```
plot_net(
  gr,
  community = NULL,
  color_map = NULL,
  extract_lcc = TRUE,
  heavy_edge_deg_perc = 0.97,
  coord = NULL,
  vsize_func = function(deg) log(deg + 3) * 1,
  vertex_border = FALSE,
  niter = 1000,
  vertex_alpha = 0.4,
```

```
  remove_loops = TRUE,
  make_simple = FALSE,
  ...
)
```

## Arguments

| | |
|---|---|
| gr | the network as an igraph object |
| community | community assignment; vector of node labels |
| color_map | color palette for clusters in 'gr' |
| extract_lcc | Extract largest connected component or not |
| heavy_edge_deg_perc | Degree percentile threshold for determining heavy edges |
| coord | Optional starting positions for the vertices. If this argument is not NULL then it should be an appropriate matrix of starting coordinates. |
| vsize_func | function to determine the size of node size |
| vertex_border | whether to show the border of vertex or not |
| niter | number of iteration for FR layout computation |
| vertex_alpha | factor modifying the opacity alpha of vertex; typically in [0,1] |
| remove_loops | whether to remove loops in the network |
| make_simple | whether to simplify edge weight calculation |
| ... | other settings |

## Value

A network plot

---

# plot_roc *Plot ROC curves*

---

## Description

Plot ROC curves given results from simulate_roc.

## Usage

```
plot_roc(roc_results, method_names = NULL, font_size = 16)
```

## Arguments

| | |
|---|---|
| roc_results | data frame roc from the output list of simulate_roc |
| method_names | a list of method names |
| font_size | font size of the plot |

## Value

Roc plot based on results from simulate_roc

## plot_smooth_profile *Plot community profiles*

### Description

Plot the smooth community profiles based on a resampled statistic

### Usage

```
plot_smooth_profile(
  tstat,
  net_name = "",
  trunc_type = "none",
  spar = 0.3,
  plot_null_spar = TRUE,
  alpha = 0.3,
  base_font_size = 12
)
```

### Arguments

| | |
|---|---|
| tstat | dataframe that has a column 'value' as statistic in the plot and a column 'K' as its corresponding community number |
| net_name | name of network |
| trunc_type | method to round the dip/elbow point as the estimated community number |
| spar | the sparsity level of fitting spline to the value of tstat |
| plot_null_spar | whether to plot the spline with zero sparsity |
| alpha | transparency of the points in the plot |
| base_font_size | font size of the plot |

### Value

smooth profile plot of a network

## polblogs *Political blogs network*

### Description

This is a directed network of hyperlinks between political blogs about politics in the United States of America.

## Usage

```
data(polblogs)
```

## Format

An igraph data with 1490 nodes and 19090 edges

## References

Data source. Original paper:The political blogosphere and the 2004 US election: divided they blog, Adamic, Lada A., and Natalie Glance. "." Proceedings of the 3rd international workshop on Link discovery. 2005.

---

# pp_conn *Generate planted partition (PP) connectivity matrix*

---

## Description

Create a degree-corrected planted partition connectivity matrix with a given average expected degree.

## Usage

```
pp_conn(
  n,
  oir,
  lambda,
  pri,
  theta = rep(1, n),
  normalize_theta = FALSE,
  d = rep(1, length(pri))
)
```

## Arguments

| | |
|---|---|
| n | the number of nodes |
| oir | out-in-ratio |
| lambda | the expected average degree |
| pri | the prior on community labels |
| theta | node connection propensity parameter of DCSBM |
| normalize_theta | whether to normalize theta so that max(theta) == 1 |
| d | diagonal of the connectivity matrix. An all-one vector by default. |

## Value

The connectivity matrix B of the desired DCSBM.

## printf *The usual "printf" function*

### Description

The usual "printf" function

### Usage

```
printf(...)
```

### Arguments

| | |
|---|---|
| ... | printing object |

### Value

the value of the printing object

## rsymperm *Generate random symmetric permutation matrix*

### Description

Generate a random symmetric permutation matrix (recursively)

### Usage

```
rsymperm(K)
```

### Arguments

| | |
|---|---|
| K | size of the matrix |

### Value

A random K x K symmetric permutation matrix

## sample_dcer *Sample from a DCER*

### Description

Sample an adjacency matrix from a degree-corrected Erdős–Rényi model (DCER).

### Usage

```
sample_dcer(theta)
```

### Arguments

| | |
|---|---|
| theta | Node connectivity propensity vector ($n * 1$) |

### Value

An adjacency matrix following DCSBM

## sample_dclvm *Sample from a DCLVM*

### Description

A DCLVM with $K$ clusters has edges generated as

$$E[\, A_{ij} \mid x, \theta \,] \;\propto\; \theta_i \theta_j e^{-\|x_i - x_j\|^2}$$

where $x_i = 2e_{z_i} + w_i$, $e_k$ is the $k$th basis vector of $R^d$, $w_i \sim N(0, I_d)$, and $\{z_i\} \subset [K]^n$. The proportionality constant is chosen such that the overall network has expected average degree $\lambda$. To calculate the scaling constant, we approximate $E[e^{-\|x_i - x_j\|^2}]$ for $i \neq j$ by generating random `npairs` $\{z_i, z_j\}$ and average over them.

### Usage

```
sample_dclvm(z, lambda, theta, npairs = NULL)
```

### Arguments

| | |
|---|---|
| z | a vector of cluster labels |
| lambda | desired average degree of the network |
| theta | degree parameter |
| npairs | number of pairs of $\{z_i, z_j\}$ |

## Details

Sample form a degree-corrected latent variable model with Gaussian kernel

## Value

Adjacency matrix of DCLVM

---

`sample_dcpp` *Sample from a DCPP*

---

## Description

Sample from a degree-corrected planted partition model

## Usage

```
sample_dcpp(
  n,
  lambda,
  K,
  oir,
  theta = NULL,
  pri = rep(1, K)/K,
  normalize_theta = FALSE
)
```

## Arguments

| | |
|---|---|
| `n` | number of nodes |
| `lambda` | average degree |
| `K` | number of communities |
| `oir` | out-in ratio |
| `theta` | propensity parameter, if not given will be samples from a Pareto distribution with scale parameter 2/3 and shape parameter 3 |
| `pri` | prior distribution of node labels |
| `normalize_theta` | whether to normalize theta so that max(theta) == 1 |

## Value

an adjacency matrix following a degree-corrected planted parition model

## See Also

sample_dcsbm, sample_tdcsbm

## sample_dcsbm *Sample from a DCSBM*

### Description

Sample an adjacency matrix from a degree-corrected block model (DCSBM)

### Usage

```
sample_dcsbm(z, B, theta = 1)
```

### Arguments

| | |
|---|---|
| z | Node labels ($n * 1$) |
| B | Connectivity matrix ($K * K$) |
| theta | Node connectivity propensity vector ($n * 1$) |

### Value

An adjacency matrix following DCSBM

### See Also

sample_dcpp, fast_sbm, sample_tdcsbm

### Examples

```
B = pp_conn(n = 10^3, oir = 0.1, lambda = 7, pri = rep(1,3))$B
head(sample_dcsbm(sample(1:3, 10^3, replace = TRUE), B, theta = rexp(10^3)))
```

## sample_tdcsbm *Sample truncated DCSBM (fast)*

### Description

Sample an adjacency matrix from a truncated degree-corrected block model (DCSBM) using a fast algorithm.

### Usage

```
sample_tdcsbm(z, B, theta = 1)
```

### Arguments

| | |
|---|---|
| z | Node labels ($n * 1$) |
| B | Connectivity matrix ($K * K$) |
| theta | Node connectivity propensity vector ($n * 1$) |

## Details

The function samples an adjacency matrix from a truncated DCSBM, with entries having Bernoulli distributions with mean

$$E[A_{ij}|z] = B_{z_i,z_j} \min(1, \theta_i\theta_j).$$

The approach uses the masking idea of Aiyou Chen, leading to fast sampling for sparse networks. The masking, however, truncates $\theta_i\theta_j$ to at most 1, hence we refer to it as the truncated DCSBM.

## Value

An adjacency matrix following DCSBM

## Examples

```
B = pp_conn(n = 10^4, oir = 0.1, lambda = 7, pri = rep(1,3))$B
head(sample_tdcsbm(sample(1:3, 10^4, replace = TRUE), B, theta = rexp(10^4)))
```

---

# simulate_roc *Simulate data to estimate ROC curves*

---

## Description

Simulate data from the null and alternative distributions to estimate ROC curves for a collection of methods.

## Usage

```
simulate_roc(
  apply_methods,
  gen_null_data,
  gen_alt_data,
  nruns = 100,
  core_count = parallel::detectCores() - 1,
  seed = NULL
)
```

## Arguments

| | |
|---|---|
| apply_methods | a function that returns a data.frame with columns "method", "tstat" and "twosided" |
| gen_null_data | a function that generate data under the null model |
| gen_alt_data | a function that generate data under the alternative model |
| nruns | number of simulated data from the null/alternative model |
| core_count | number of cores used in parallel computing |
| seed | seed for random simulation |

## Value

a list of result

| | |
|---|---|
| `roc` | A data frame used to plot ROC curves with columns: method, whether a two sided test, false positive rate (FPR), and true positive rate (TPR) |
| `raw` | A data frame containing raw output from null and alternative models with columns: method, statistics value, whether a two sided test, and the type of hypothesis |
| `elapsed_time` | symstem elapsed time for generating ROC data |

---

`sinkhorn_knopp` *Sinkhorn–Knopp matrix scaling*

---

## Description

Implements the Sinkhorn–Knopp algorithm for transforming a square matrix with positive entries to a stochastic matrix with given common row and column sums (e.g., a doubly stochastic matrix).

## Usage

```
sinkhorn_knopp(
  A,
  sums = rep(1, nrow(A)),
  niter = 100,
  tol = 1e-08,
  sym = FALSE,
  verb = FALSE
)
```

## Arguments

| | |
|---|---|
| `A` | input matrix |
| `sums` | desired row/column sums |
| `niter` | number of iterations |
| `tol` | convergence tolerance |
| `sym` | whether to compute symmetric scaling D A D |
| `verb` | whether to print the current change |

## Details

Computes diagonal matrices D1 and D2 to make D1*A*D2 into a matrix with given row/column sums. For a symmetric matrix `A`, one can set `sym = TRUE` to compute a symmetric scaling D*A*D.

## Value

Diagonal matrices D1 and D2 to make D1*A*D2 into a matrix with given row/column sums.

## snac_resample *Resampled SNAC+*

### Description

Compute SNAC+ with resampling

### Usage

```
snac_resample(
  A,
  nrep = 20,
  Kmin = 1,
  Kmax = 13,
  ncores = parallel::detectCores() - 1,
  seed = 1234
)
```

### Arguments

| | |
|---|---|
| A | adjacency matrix |
| nrep | number of times SNAC+ is computed |
| Kmin | minimum community number to use in SNAC+ |
| Kmax | maximum community number to use in SNAC+ |
| ncores | number of cores to use in the parallel computing |
| seed | seed for random sampling |

### Value

A data frame with columns specifying repetition cycles, number of community numbers and the value of SNAC+ statistics

## snac_select *Estimate community number with SNAC+*

### Description

Applying SNAC+ test sequentially to estimate community number of a network fit to DCSBM

## Usage

```
snac_select(
  A,
  Kmin = 1,
  Kmax,
  alpha = 1e-05,
  labels = NULL,
  cluster_fct = spec_clust,
  ...
)
```

## Arguments

| | |
|---|---|
| A | adjacency matrix. |
| Kmin | minimum candidate community number. |
| Kmax | maximum candidate community number. |
| alpha | significance level for rejecting the null hypothesis. |
| labels | a matrix with each column being a row label vector for a candidate community number. If not provided, will be computed by cluster_fct. |
| cluster_fct | community detection function to get label vectors to compute SNAC+ statistics (in snac_test), by default using spec_clust. |
| ... | additional arguments for cluster_fct. |

## Value

estimated community number.

## See Also

snac_test

## Examples

```
A <- sample_dcpp(500, 10, 3, 0.1)$adj
snac_select(A, Kmax = 6)
```

---

# snac_test *SNAC test*

---

## Description

The SNAC test to measure the goodness-of-fit of the DCSBM to network data.

The function computes the SNAC+ or SNAC statistics in the paper below. The row label vector of the adjacency matrix could be given through z otherwise will be estimated by cluster_fct. One can specify the ratio of nodes used to estimate column label vector. If plus = TRUE, the column labels will be estimated by spec_clust with (K+1) clusters, i.e. performing SNAC+ test, otherwise with K clusters SNAC test. One can also get multiple test statistics with repeated random subsampling on nodes.

## Usage

```
snac_test(
  A,
  K,
  z = NULL,
  ratio = 0.5,
  fromEachCommunity = TRUE,
  plus = TRUE,
  cluster_fct = spec_clust,
  nrep = 1,
  ...
)
```

## Arguments

| | |
|---|---|
| A | adjacency matrix. |
| K | desired number of communities. |
| z | label vector for rows of adjacency matrix. If not provided, will be estimated by cluster_fct |
| ratio | ratio of subsampled nodes from the network. |
| fromEachCommunity | whether subsample from each estimated community or the full network, default is TRUE |
| plus | whether or not use column label vector with (K+1) communities to compute the statistics, default is TRUE. |
| cluster_fct | community detection function to estimate label vectors, by default using spec_clust. The first two arguments have to be A and K. |
| nrep | number of times the statistics are computed. |
| ... | additional arguments for cluster_fct. |

## Value

A list of result

| | |
|---|---|
| stat | SNAC or SNAC+ test statistic. |
| z | row label vector. |

## References

Adjusted chi-square test for degree-corrected block models, Linfan Zhang, Arash A. Amini, arXiv preprint arXiv:2012.15047, 2020.

## See Also

nac_test

## Examples

```
A <- sample_dcpp(500, 10, 4, 0.1)$adj
snac_test(A, K = 4, niter = 3)$stat
```

---

`spec_clust` *Spectral clustering (fast)*

---

## Description

Perform spectral clustering (with regularization) to estimate communities

## Usage

```
spec_clust(
  A,
  K,
  type = "lap",
  tau = 0.25,
  nstart = 20,
  niter = 10,
  ignore_first_col = FALSE
)
```

## Arguments

| | |
|---|---|
| `A` | Adjacency matrix (n x n) |
| `K` | Number of communities |
| `type` | ("lap" \| "adj" \| "adj2") Whether to use Laplacian or adjacency-based spectral clustering |
| `tau` | Regularization parameter for the Laplacian |
| `nstart` | argument from function 'kmeans' |
| `niter` | argument from function 'kmeans' |
| `ignore_first_col` | whether to ignore the first eigen vector when doing spectral clustering |

## Value

A label vector of size n x 1 with elements in 1,2,...,K

spec_repr *Spectral Representation*

## Description

Provides a spectral representation of the network (with regularization) based on the adjacency or Laplacian matrices

## Usage

```
spec_repr(A, K, type = "lap", tau = 0.25, ignore_first_col = FALSE)
```

## Arguments

| | |
|---|---|
| A | Adjacency matrix (n x n) |
| K | Number of communities |
| type | ("lap" \| "adj" \| "adj2") Whether to use Laplacian or adjacency-based spectral clustering |
| tau | Regularization parameter for the Laplacian |
| ignore_first_col | whether to ignore the first eigen vector |

## Value

The n x K matrix resulting from a spectral embedding of the network into R^K

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